Assignment 7

due date: Monday, October 15th, 2007.

The following is a list of some drill questions. As your homework, please solve the two problems marked with (*) and Problems 48, 49, and 50, pages 25-26 in your textbook.

Show that the following are equivalence relations:

- 1. equality relation between elements of any set,
- 2. "has the same birthday as" on the set of all people,
- 3. "is similar to" on the set of all triangles,
- 4. "has the same image under a function" on the elements of the domain of the function,
- 5. "is congruent modulo n" on the set of integers,
- 6. "is parallel to" on the set of lines on the plane,
- 7. similarity on the set of well-orderings,
- 8. let $a, b, c, d \in \mathbb{N}$, and (a, b) and (c, d) be ordered pairs; the relations are $(a, b) \sim (c, d)$ if a + d = b + c, and $(a, b) \sim (c, d)$ if ad = bc,
- 9. (*) let $(r_n), (s_n)$ be any two Cauchy sequences of rational numbers; the relation is $(r_n) \sim (s_n)$ if the sequence $(r_n s_n)$ has limit 0.

In each case describe the equivalence classes.

Explain why the following relations are **not** equivalences:

- 1. the relation "\ge " between the real numbers,
- 2. (*) the relation "has a common factor greater than 1 with" on the set of integers greater than 1,
- 3. the relation "is a sibling of" on the set of all humans,